

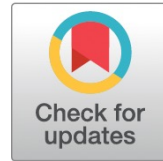


มหาวิทยาลัยมหิดล  
คณะแพทยศาสตร์โรงพยาบาลรามาธิบดี

Department of Clinical Epidemiology and Biostatistics



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**ORIGINAL ARTICLE**

**Choice of imputation method for missing metastatic status affected estimates of metastatic prostate cancer incidence**

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**Commented by Sureerat Suwatharangkoon**

October 6, 2023



# Types of missing data

## Missing completely at random (MCAR)

- *The probability of being missing is the same for all cases*

## Missing at random (MAR)



Multiple imputation

- *The missingness depends on information we have already observed*

## Missing not at random (MNAR)



Sensitivity analyses

- *The probability that data are missing depends on the **unobserved data***



# Proposed methods for dealing with missing data in the design phase

- Optimizing data collection
- Pilot studies can help to identify variables particularly susceptible to missing values, and steps
- Regular monitoring of data quality and completeness
- Patients may be asked to provide reasons for refusing to participate



# Proposed methods for dealing with missing data in the analytic phase

Methods	Brief description	Assumption to achieve unbiased estimates	Advantages	Limitation(s)
Complete-case analysis	Include only individuals with complete information on all variables in the dataset	MCAR	<ul style="list-style-type: none"> <li>• Simplicity</li> <li>• Comparability across analyses</li> </ul>	<ul style="list-style-type: none"> <li>• Data may not be representative. Reduction of sample size and thereby of statistical power</li> <li>• Too large standard error (lack of precision of the results)</li> <li>• Discarding valuable data</li> </ul>
Missing indicator method	For categorical variables, missing values are grouped into a “missing” category. For continuous variables, missing values are set to a fixed value (usually zero), and an extra indicator or dummy (1/0) variable is added to the main analytic model to indicate whether the value for that variable is missing	None	<ul style="list-style-type: none"> <li>• Uses all available information about missing observation and retains the full dataset</li> </ul>	<ul style="list-style-type: none"> <li>• The magnitude and direction of bias difficult to predict</li> <li>• Too small standard error</li> <li>• The results may be meaningless since method is not theoretically driven</li> <li>• Bias due to residual confounding</li> </ul>



Methods	Brief description	Assumption to achieve unbiased estimates	Advantages	Limitation(s)
Single value imputation	Replace missing values by a single value (eg, mean score of the observed values or the most recently observed value for a given variable if data are measured longitudinally)	MCAR, only when estimating mean	<ul style="list-style-type: none"> <li>• Run analyses as if data are complete</li> <li>• Retains full dataset</li> </ul>	<ul style="list-style-type: none"> <li>• Too small standard error (overestimation of precision of the results)</li> <li>• Potentially biased results</li> <li>• Weakens covariance and correlation estimates in the data (ignores relationship between variables)</li> </ul>
Sensitivity analyses with worst- and best-case scenarios	Missing data values are replaced with the highest or lowest value observed in the dataset	MCAR	<ul style="list-style-type: none"> <li>• Simplicity</li> <li>• Retains full dataset</li> </ul>	<ul style="list-style-type: none"> <li>• Too small standard error and thereby overestimation of precision of the results</li> <li>• Analyses yielding opposite results may be difficult to interpret</li> </ul>
Multiple imputation	Missing data values are imputed based on the distribution of other variables in the dataset	MAR (but can handle both MCAR and MNAR)	<ul style="list-style-type: none"> <li>• Variability more accurate for each missing value since it considers variability due to sampling and due to imputation (standard error close to that of having full dataset with true values)</li> </ul>	<ul style="list-style-type: none"> <li>• Room for error when specifying models</li> </ul>



# Specification of imputation models

1. Deterministic imputation
2. Partial deterministic imputation + MI (PDI + MI)
3. Standard MI (SMI)
4. Restricted MI (RMI)

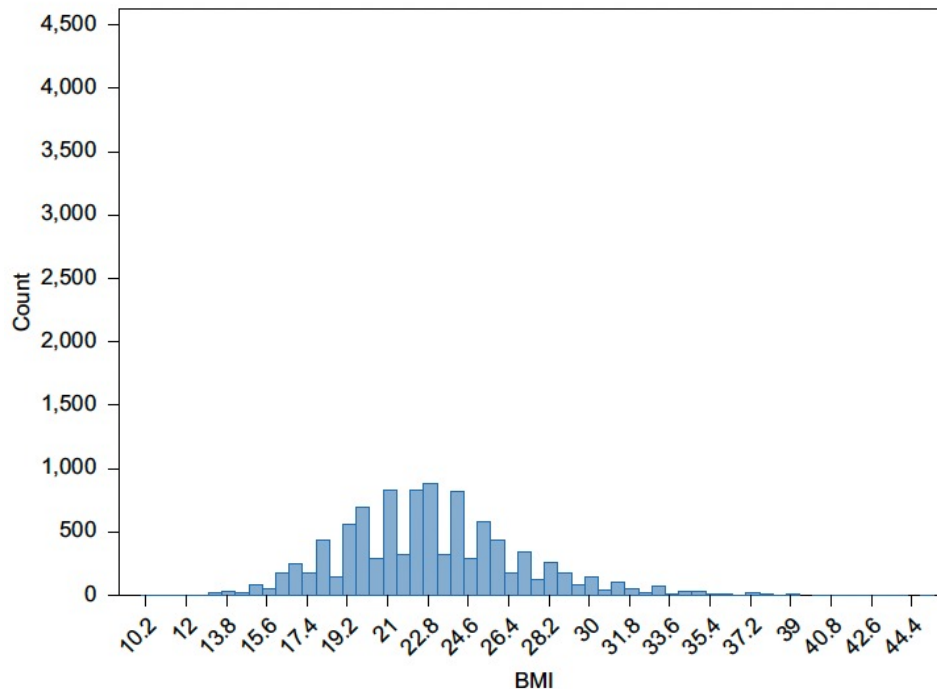


# 1. Deterministic imputation

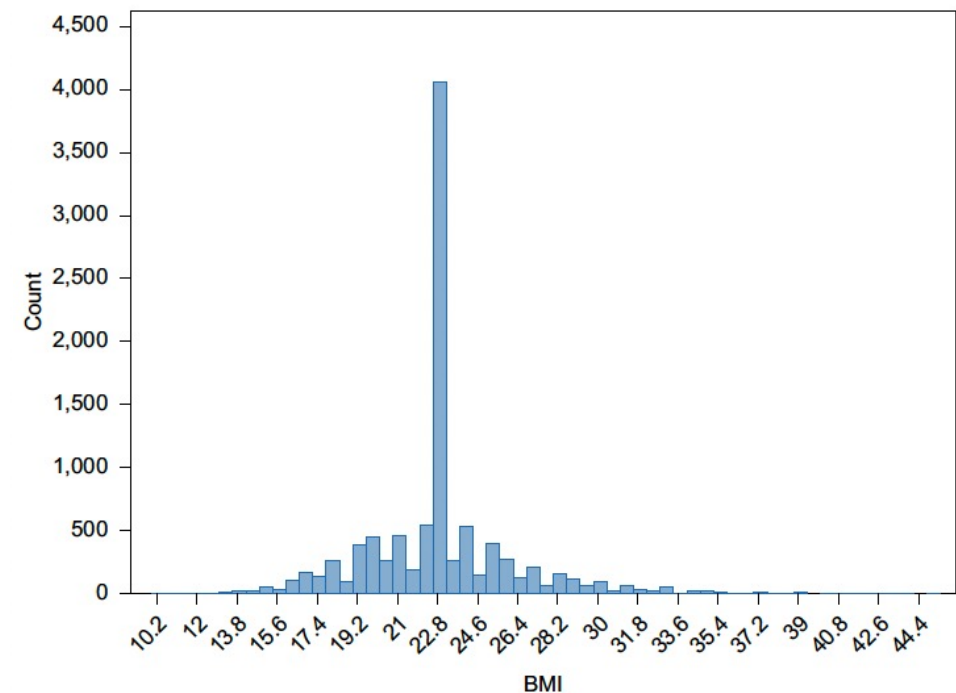
- Substitution method (**missing M stage -> M0**)
- Imaged men with M0 cannot be differentiated from nonimaged men
- Unbiased estimates for the population means or totals if
  - the missing values are missing completely at random (MCAR)
  - the missing values only depend on the auxiliary variables which are used to construct the imputation cells



# Single value imputation



Normal distribution of observed BMI in a full dataset of 10,000 observations.



Distribution of BMI in a dataset of 10,000 observations, where 35% of BMI values are missing and replaced by the observed mean BMI value





# 1. Deterministic imputation

- However, the distribution of the data will be distorted substantially and the concentration of all imputed values at the cell means creates spikes in the distribution.
- Therefore, quartile estimates will be biased, and the variances materially underestimated.



# 1. Deterministic imputation


- Variance-covariance estimates calculation by the adjusted mean imputation (or substitution) method
- Using a denominator of  $n-m-1$  instead of  $n-1$   
( $n$  = sample size,  $m$  = number of cases missing)



# 1. Deterministic imputation

- Cohen (1996) suggested another way to adjust variance estimates by imputing more diversified values for the missing cases.

- Imputing half of the missing values with


$$\bar{y}_r + \sqrt{\frac{n+r-1}{r-1}} D_r$$
$$\bar{y}_r - \sqrt{\frac{n+r-1}{r-1}} D_r$$

$r$  = number of response values,  $\bar{y}_r$  = mean of observed values,

$$D_r^2 = \frac{1}{r} \sum_{i=1}^r (y_i - \bar{y}_r)^2$$



Methods	Brief description	Assumption to achieve unbiased estimates	Advantages	Limitation(s)
Single value imputation	Replace missing values by a single value (eg, mean score of the observed values or the most recently observed value for a given variable if data are measured longitudinally)	MCAR, only when estimating mean	<ul style="list-style-type: none"><li>• Run analyses as if data are complete</li><li>• Retains full dataset</li></ul>	<ul style="list-style-type: none"><li>• Too small standard error (overestimation of precision of the results)</li><li>• Potentially biased results</li><li>• Weakens covariance and correlation estimates in the data (ignores relationship between variables)</li></ul>



## 2. Partial deterministic imputation + MI (PDI + MI)

- **PDI**: Low metastatic risk with missing M stage -> M0
- **MI**: Remaining missing data in M stage and all other variables (e.g., PSA and N stage) was imputed using MI including all variables.



## 2. Partial deterministic imputation + MI (PDI + MI)

The following variables were included: age at diagnosis, year of diagnosis, and M stage, and the auxiliary variables

- logPSA, T and N stage, Gleason sum, WHO grade, primary treatment, mode of detection, follow-up time and cause of death (prostate cancer or other causes) or censoring.



# Imputation based on Clinical Imputation

- Imputation missing N- and M-stage data only in low/intermediate-risk men

For example:

- **T1 and Gleason 6** -> unlikely to have nodal involvement or distant metastases (**N0 and M0**)
- **Staging data is available for nodal disease** but missing data for distant metastases -> likely that staging was performed and very low likelihood of missing M-stage representing positive disease (**M0**)

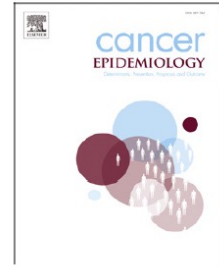


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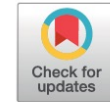
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# Cancer Epidemiology

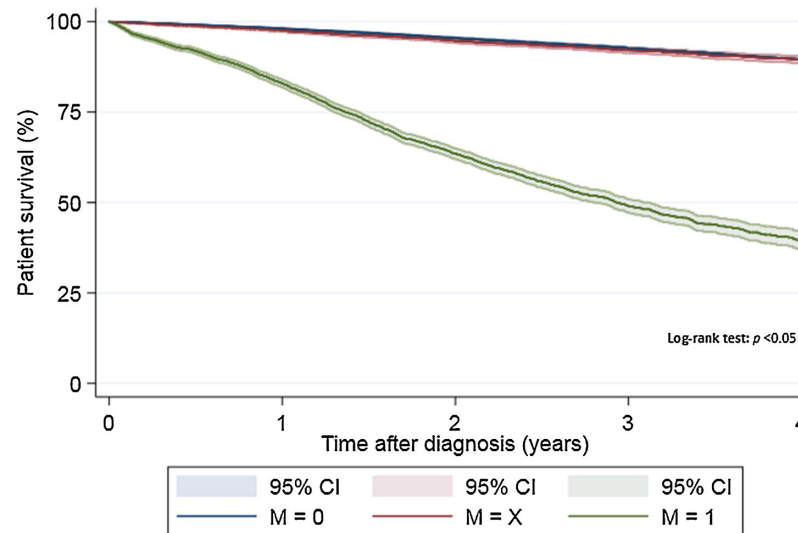
journal homepage: [www.elsevier.com/locate/canep](https://www.elsevier.com/locate/canep)



## Imputation of missing prostate cancer stage in English cancer registry data based on clinical assumptions



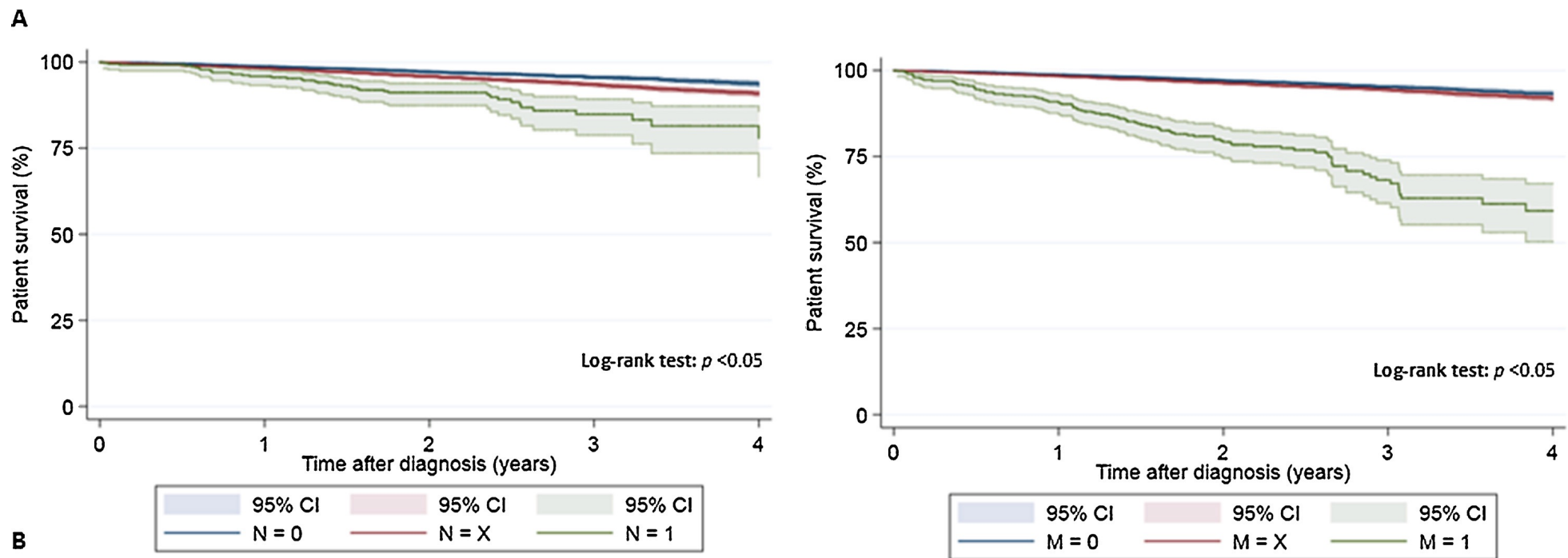
Matthew G. Parry<sup>a,b,\*</sup>, Arunan Sujenthiran<sup>b</sup>, Thomas E. Cowling<sup>a,b</sup>, Susan Charman<sup>b</sup>, Julie Nossiter<sup>a,b</sup>, Ajay Aggarwal<sup>a,c,d</sup>, Noel W. Clarke<sup>e,f</sup>, Heather Payne<sup>g</sup>, Jan van der Meulen<sup>a,b</sup>



\*Note: Patient survival for men with M0 (blue line) or MX (red line) was very similar with narrow and overlapping confidence intervals (95%). Both lines therefore appear superimposed.

Overall survival for men with **complete N-stage (N1/N0)** showing the distribution of M-stage (M1/M0/missing M).

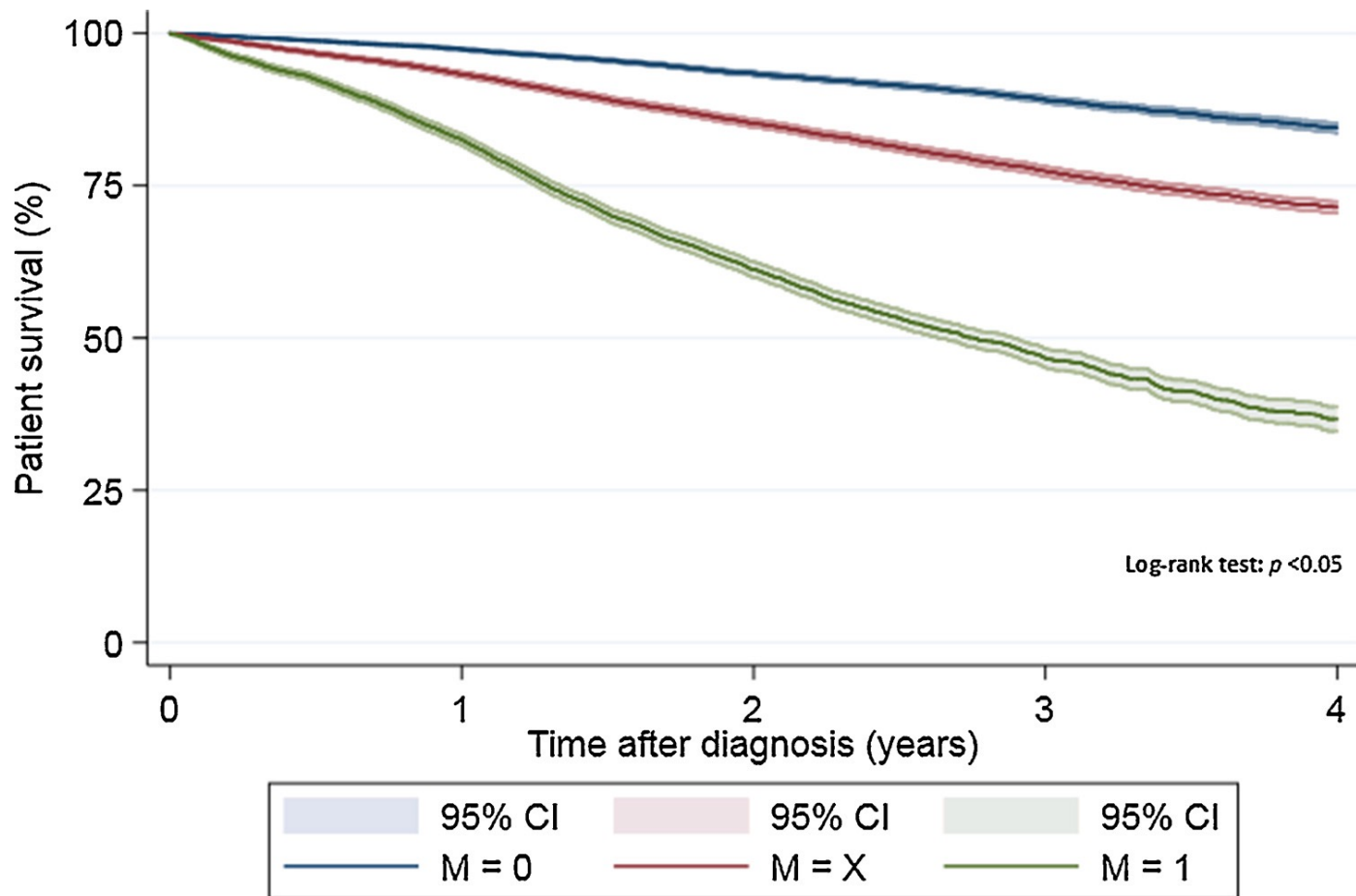




Overall survival for men with **low/intermediate-risk disease** (T1-2 and Gleason score  $\leq 7$ ) showing the distribution of: a. N-stage (N1/N0/missing N) b. M-stage (M1/M0/missing M)

### 3 clinical assumptions:

1. Recorded N-stage: missing M-stage  $\rightarrow$  M0
2. Low/Intermediate-risk men: missing M-stage  $\rightarrow$  M0
3. Low/Intermediate-risk men: missing N-stage  $\rightarrow$  N0



Overall survival for men with **high-risk disease** (T3-4 or Gleason score  $\geq 8$ ) showing the distribution of M-stage (M1/M0/missing M).



## 2. Partial deterministic imputation + MI (PDI + MI)

- Increased the completeness of clinical staging
- Perform as well as multiple imputation
- More easily applicable for those without appropriate statistical software or expertise
- Less appropriate for use in cancer registries with less complete staging data



## 3. Standard MI

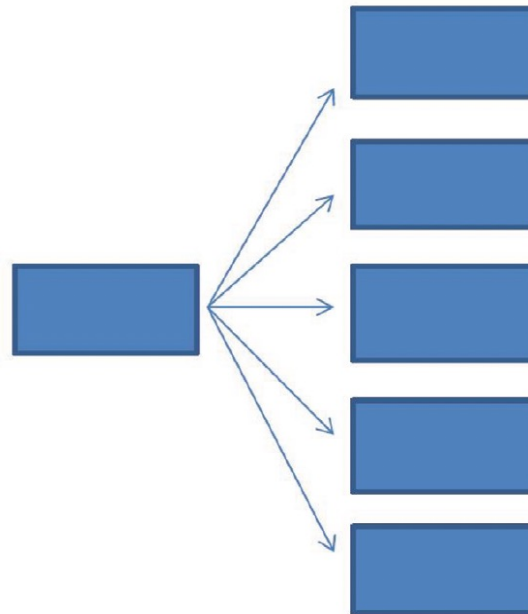
- All variables were included and missing data were imputed using MI.
- This model was identical to PDI + MI. The only difference was that M stage was not substituted to M0 prior to performing the multiple imputation procedure.



# The 3 main stages of implementing MI

## Imputation

The first stage



Incomplete dataset

Multiple copies of imputed datasets



# An example of the imputed missing BMI values generated with 5 imputed datasets

Patient number	Imputed data set 1 (BMI 1)	Imputed data set 2 (BMI 2)	Imputed data set 3 (BMI 3)	Imputed data set 4 (BMI 4)	Imputed data set 5 (BMI 5)
10	25.3	26.4	27.0	24.8	29.7
25	19.7	21.3	22.3	20.5	23.8
23	22.1	27.6	22.9	28.1	25.8
150	20.1	22.5	23.4	21.7	23.0
175	19.7	20.2	21.2	22.4	21.9

**Abbreviation:** BMI, body mass index.



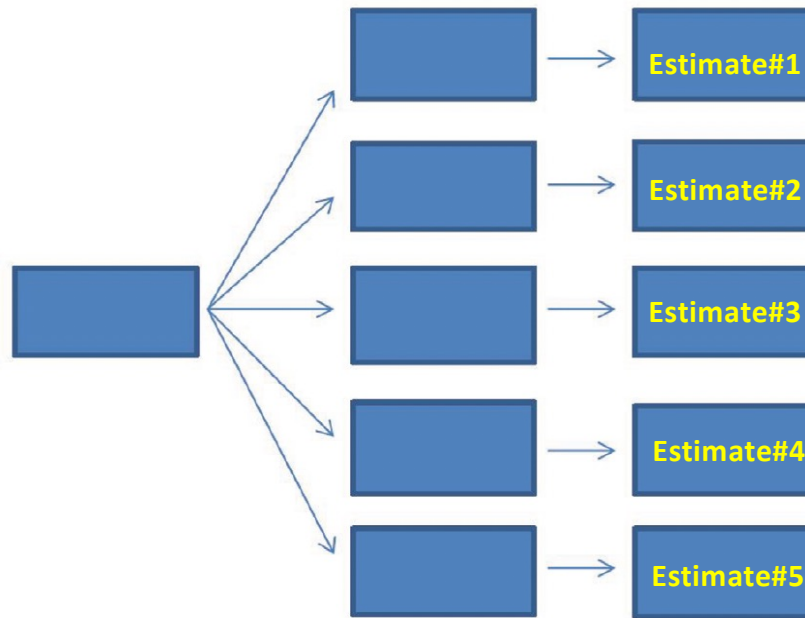
# The 3 main stages of implementing MI

## Imputation

The first stage

## Analysis

The second stage



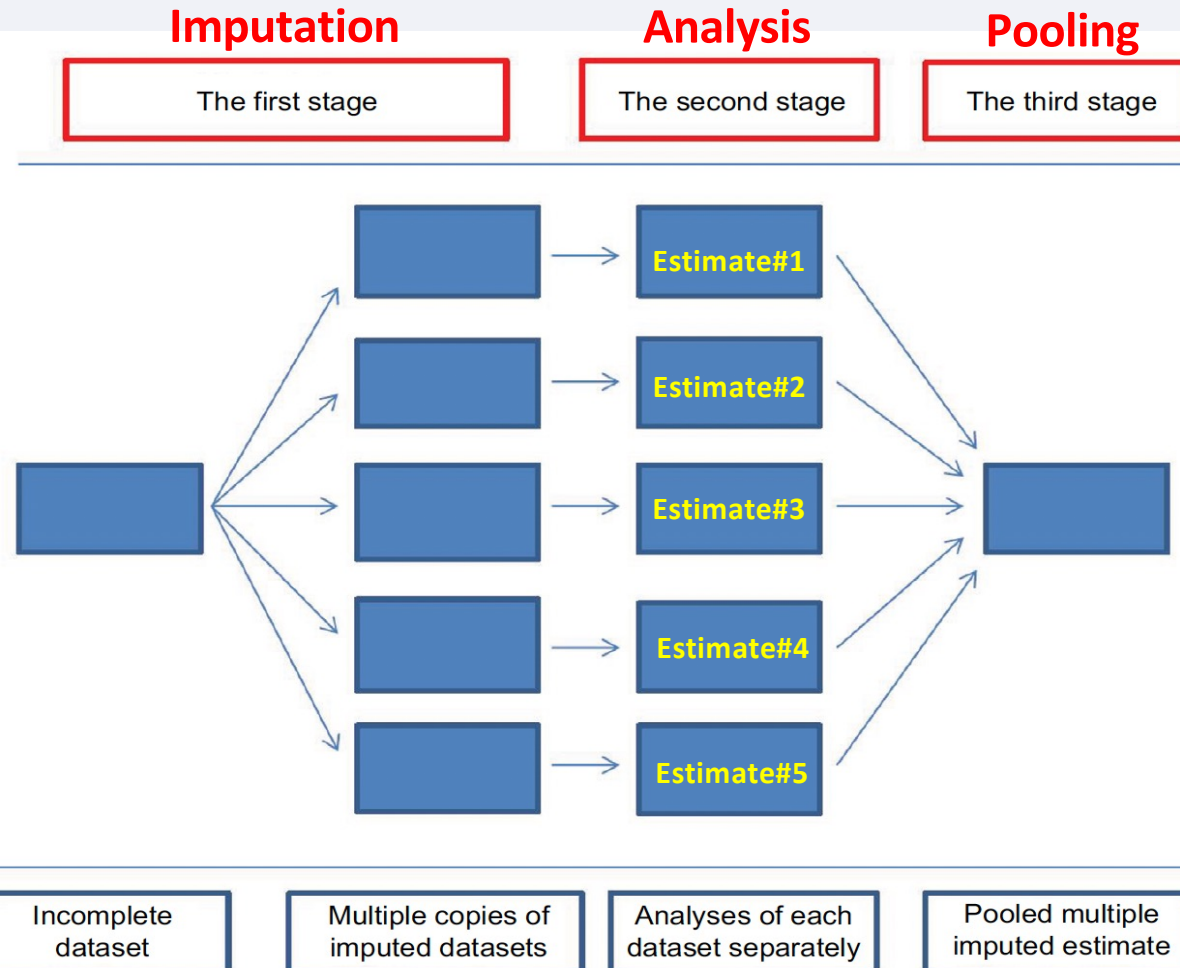
Incomplete dataset

Multiple copies of imputed datasets

Analyses of each dataset separately



# The 3 main stages of implementing MI







# Missing at random (MAR) assumption

- The validity of the MI methods relies on the plausibility of the MAR assumption
- T- tests and logistic regression analyses can be used to investigate if there is a relationship between variables with and without missing data
- MNAR can result in a large bias in estimates obtained after MI that operates under the MAR assumption



## Oncology: Prostate/Testis/Penis/Urethra

### Bias Due to Missing SEER Data in D'Amico Risk Stratification of Prostate Cancer

D'Amico staging requires all 3 variables

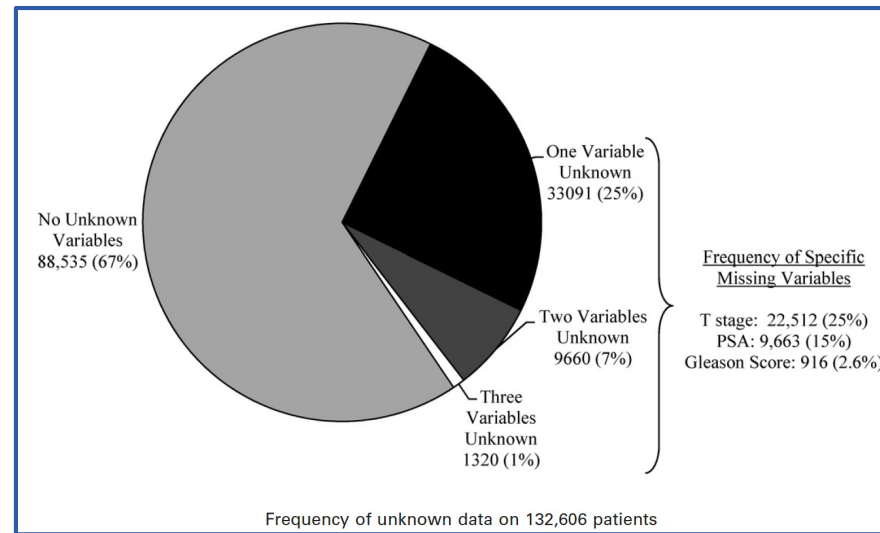
- Prostate specific antigen (PSA)
- T stage
- Gleason score

**P:** men with incident prostate cancer  
**E:** patient age, race, Geographic region  
**O:** *unclassified risk group* due to unknown variables

**Table 1.** Low, intermediate and high risk cT stage, PSA and Gleason score when other clinical variables were known vs unknown

Other Known Variable D'Amico Risk Strata*	No. T Stage (%)		No. PSA (%)		No. Gleason Score (%)	
	Known	Unknown	Known	Unknown	Known	Unknown
T stage:						
T2a or Less	—	—	64,477 (78)	8,283 (85)	82,488 (74)	977 (65)
T2b	—	—	2,525 (3)	175 (2)	17,602 (16)	240 (16)
T2c or Greater	—	—	15,723 (19)	1340 (14)	10,997 (10)	277 (19)
PSA (ng/dl):						
Less than 10	66,510 (74)	16,915 (73)	—	—	78,643 (80)	1,278 (86)
10–20	14,289 (16)	3,553 (15)	—	—	2,657 (3)	43 (3)
Greater than 20	8,652 (10)	2,622 (11)	—	—	16,898 (17)	165 (11)
Gleason score:						
2–6	50,501 (51)	15,536 (50)	55,887 (50)	10,150 (56)	—	—
7	34,962 (36)	11,133 (36)	40,600 (37)	5,495 (30)	—	—
8–10	12,735 (13)	4,355 (14)	14,560 (13)	2,530 (14)	—	—

\* Cells in each 3 × 2 box do not sum to total cohort due to multiple exclusions, ie if T stage was known and PSA unknown, patient is not shown in any PSA cell for T stage known column but may appear in Gleason score cell in T stage known column.



**Table 2.** Unclassified DARG due to unknown variables by patient age and race

	No. Pts (% unclassified DARG)	Unclassified DARG Adjusted OR (95% CI)	Probability Greater Than Chi-Square
<b>Age:</b>			
Less than 45	805 (32.2)	1.1 (1.0–1.3)	0.0801
45–54	11,757 (30.5)	1.1 (1.0–1.1)	0.0346
55–64	40,400 (29.3)	1.0 (referent)	—
65–74	48,066 (31.1)	1.1 (1.1–1.1)	<0.0001
75–84	27,135 (40.4)	1.5 (1.5–1.6)	<0.0001
85 or Greater	4,408 (55.8)	2.4 (2.3–2.6)	<0.0001
Unknown	35 (80)	6.6 (2.8–15.3)	<0.0001
<b>Race:</b>			
NonHispanic white	94,270 (33.2)	1.0 (referent)	—
NonHispanic black	15,093 (29.2)	0.8 (0.8–0.9)	<0.0001
Hispanic	11,722 (33.3)	1.1 (1.1–1.2)	<0.0001
Asian/Pacific Islanders	6,278 (27.1)	1.0 (0.9–1.0)	0.1188
AI/AN/other/unknown	5,243 (53.0)	2.4 (2.2–2.5)	<0.0001



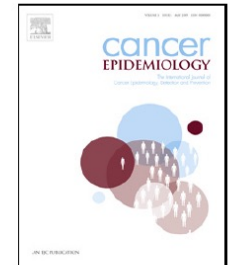
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## Cancer Epidemiology

The International Journal of Cancer Epidemiology, Detection, and Prevention

journal homepage: [www.cancerepidemiology.net](http://www.cancerepidemiology.net)



### Characteristics of cases with unknown stage prostate cancer in a population-based cancer registry

Qingwei Luo<sup>a,b,\*</sup>, Xue Qin Yu<sup>a,b</sup>, Claire Cooke-Yarborough<sup>c</sup>,  
David P. Smith<sup>a,d</sup>, Dianne L. O'Connell<sup>a,b,e,f</sup>

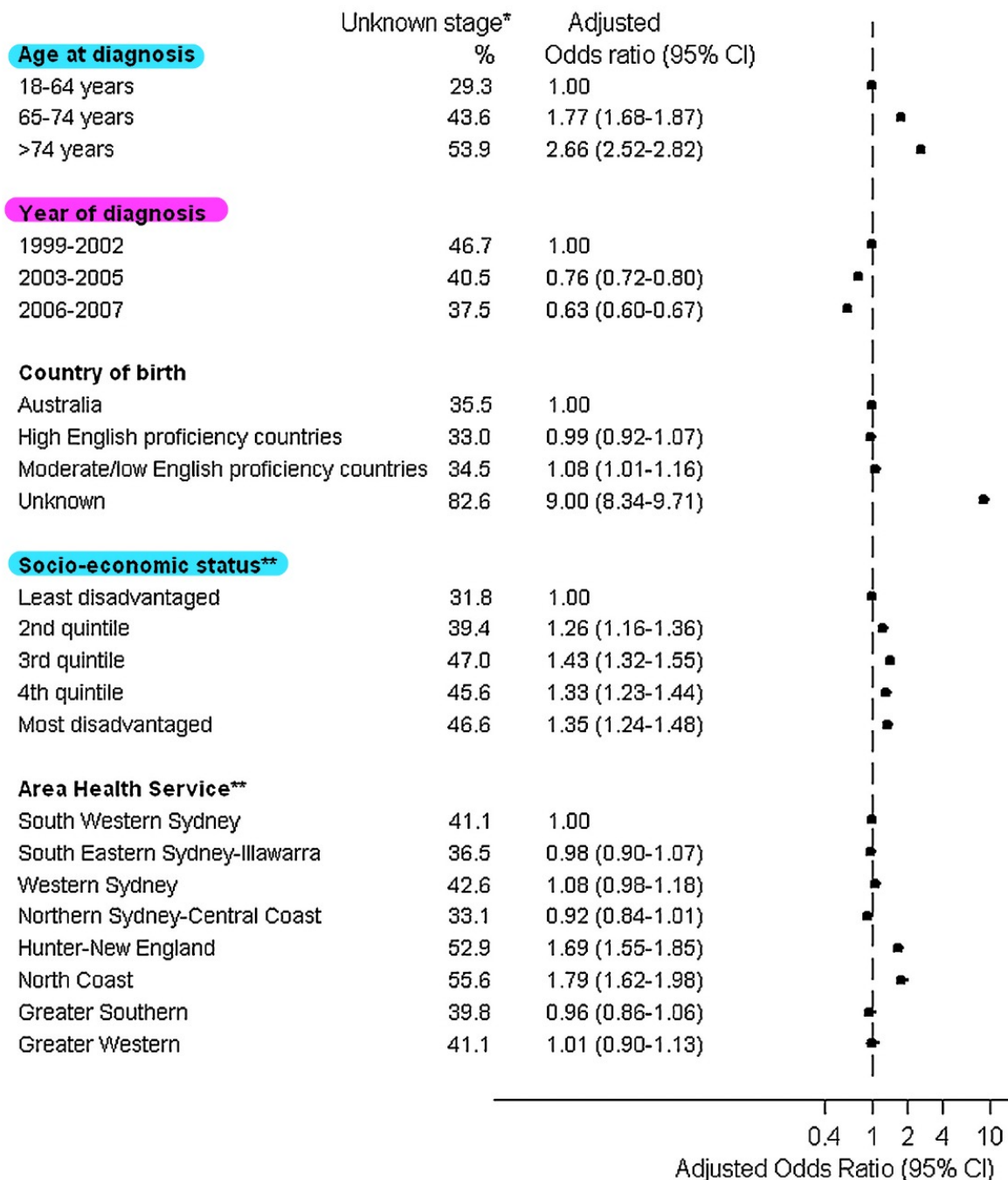
**P: Primary prostate cancer cases from New South Wales Central Cancer Registry (NSW CCR)**

**E: Patient characteristics**

- age, place of residence at diagnosis, year of diagnosis and country of birth

**O: Disease stage of prostate cancer**

- localized, regional, distant or “unknown”



\* Unknown stage recorded by the NSW Central Cancer Registry

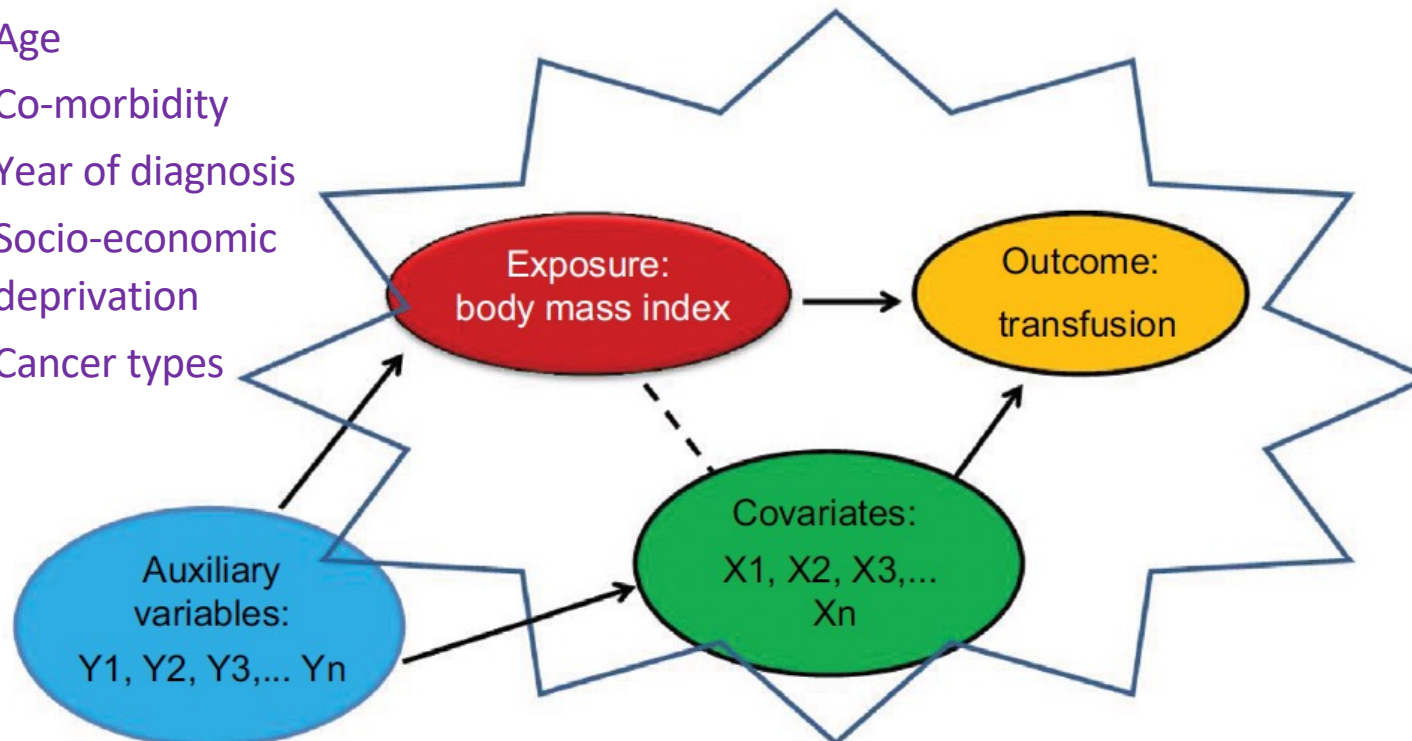
\*\* Area Health Service and Socio-economic status were based on the case's place of residence at diagnosis



# Selection of variables

in order to create multiple imputed datasets  
when looking into the association BMI and transfusion risk.

- Age
- Co-morbidity
- Year of diagnosis
- Socio-economic deprivation
- Cancer types



Selection of variables to create multiple imputed datasets:

Auxiliary variables

The variables that are in the subsequent analysis model (exposure, covariates, and outcome)

variables within the original data that are not included in the analysis, but are correlated to the variables of interest or help to keep the missing process random



# Which variables should be included in the multiple imputation model?

Auxiliary variables need to fulfill one of following criteria

- 1) The auxiliary variable should be associated with the values of the incomplete variables
- 2) The auxiliary variable should be associated with the value of the incomplete variables and the likelihood of the data being missing



# Which variables should be included in the multiple imputation model?

If we are not sure, these relationships can be identified by setting up,

- 1) a logistic regression model with the missingness (as 0 or 1) being the outcome and auxiliary variables being the explanatory variables, or
- 2) a regression model with the incomplete variable as the outcome and auxiliary variables again as explanatory variables.





## 4. Restricted MI

- Only TNM stage, age, and year of diagnosis were included, and missing data were imputed using MI.
- In particular, PSA, Gleason score, survival time and indicator of cause of death (or censoring) were omitted from the imputation model.
- Survival data were included in a sensitivity analysis.



# Multiple imputation example

**Table 4** Association between BMI and risk of blood transfusion adjusted for age and gender


Patient characteristics	Full data (n=3,500)			Complete case analysis (n=2,733) <sup>767 (22%) with missing</sup>			Multiple imputation (n=3500, m=5)			Multiple imputation (n=3500, m=30)		
	OR	SE	95% CI	OR	SE	95% CI	OR	SE	95% CI	OR	SE	95% CI
BMI	0.980	0.0085	(0.963, 0.997)	0.978	0.0098	(0.959, 0.997)	0.976	0.0087	(0.959, 0.994)	0.978	0.0098	(0.959, 0.997)
Age (years)	Baseline											
<75	Baseline											
≥75	2.100	0.1928	(1.754, 2.514)	2.244	0.2421	(1.816, 2.772)	2.097	0.1927	(1.752, 2.511)	2.098	0.1928	(1.752, 2.511)
Gender	Baseline											
Female	Baseline											
Male	0.815	0.0630	(0.700, 0.948)	0.906	0.0779	(0.765, 1.072)	0.818	0.0633	(0.702, 0.952)	0.817	0.0634	(0.702, 0.951)

**Note:** Results are presented for full-observed data, complete-case analysis, and multiple imputation and contain point estimates for ORs, SEs, and 95% CIs.

**Abbreviations:** BMI, body mass index; CI, confidence interval; OR, odds ratio; SE, standard error.



Methods	Brief description	Assumption to achieve unbiased estimates	Advantages	Limitation(s)
Single value imputation	Replace missing values by a single value (eg, mean score of the observed values or the most recently observed value for a given variable if data are measured longitudinally)	MCAR, only when estimating mean	<ul style="list-style-type: none"> <li>• Run analyses as if data are complete</li> <li>• Retains full dataset</li> </ul>	<ul style="list-style-type: none"> <li>• Too small standard error (overestimation of precision of the results)</li> <li>• Potentially biased results</li> <li>• Weakens covariance and correlation estimates in the data (ignores relationship between variables)</li> </ul>
Partial deterministic imputation + Multiple imputation	Replacing missing values by a single value, and then remaining missing data values are imputed using multiple imputation based on the distribution in the dataset	MAR	<ul style="list-style-type: none"> <li>• Increased the completeness of clinical staging</li> <li>• Perform as well as multiple imputation</li> <li>• More easily applicable for those without appropriate statistical software or expertise</li> </ul>	<ul style="list-style-type: none"> <li>• Less appropriate for use in cancer registries with less complete staging data</li> </ul>
Multiple imputation	Missing data values are imputed based on the distribution of other variables in the dataset	MAR (but can handle both MCAR and MNAR)	<ul style="list-style-type: none"> <li>• Variability more accurate for each missing value since it considers variability due to sampling and due to imputation (standard error close to that of having full dataset with true values)</li> </ul>	<ul style="list-style-type: none"> <li>• Room for error when specifying models</li> </ul>

A hand is shown holding a stack of five wooden blocks. The blocks are stacked vertically and contain the text 'THANK YOU FOR YOUR ATTENTION' from top to bottom. The top block is light-colored wood, the second and third are medium-colored wood, the fourth is white, and the bottom block is light-colored wood. The background is a solid dark blue color. A faint 'dreamstime.' watermark is visible across the middle of the stack.

**THANK**

**YOU**

**FOR**

**YOUR**

**ATTENTION**